

4. (a) Show that $x^2+6x+11$ can be written as

$$(x+p)^2+q$$

where p and q are integers to be found.

(2)

(b) In the space at the top of page 7, sketch the curve with equation $y = x^2 + 6x + 11$, showing clearly any intersections with the coordinate axes.

(2)

(c) Find the value of the discriminant of $x^2+6x+11$

(2)



Question 4 continued

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(Total 6 marks)

Q4

7

Turn over



6.

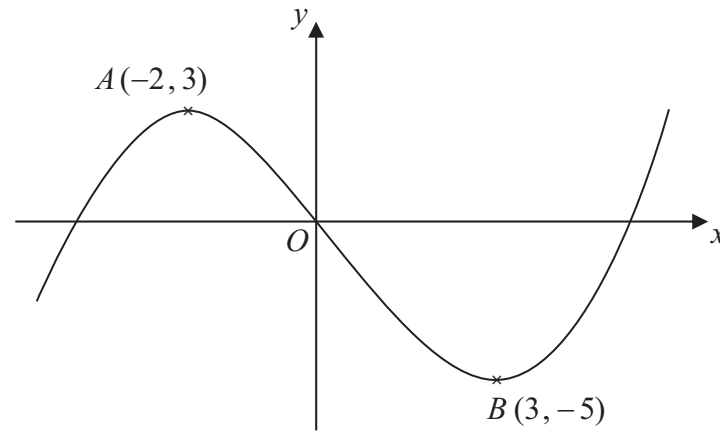


Figure 1

Figure 1 shows a sketch of the curve with equation $y = f(x)$. The curve has a maximum point A at $(-2, 3)$ and a minimum point B at $(3, -5)$.

On separate diagrams sketch the curve with equation

(a) $y = f(x+3)$ **(3)**

(b) $y = 2f(x)$ **(3)**

On each diagram show clearly the coordinates of the maximum and minimum points.

The graph of $y = f(x)+a$ has a minimum at $(3, 0)$, where a is a constant.

(c) Write down the value of a . **(1)**



Question 6 continued

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(Total 7 marks)

Q6



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8. (a) Find an equation of the line joining $A(7, 4)$ and $B(2, 0)$, giving your answer in the form $ax+by+c=0$, where a, b and c are integers. **(3)**

(b) Find the length of AB , leaving your answer in surd form. **(2)**

The point C has coordinates $(2, t)$, where $t > 0$, and $AC = AB$.

(c) Find the value of t . **(1)**

(d) Find the area of triangle ABC . **(2)**



Question 8 continued

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Question 9 continued

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10. (a) On the axes below sketch the graphs of

(i) $y = x(4-x)$

(ii) $y = x^2(7-x)$

showing clearly the coordinates of the points where the curves cross the coordinate axes.

(5)

(b) Show that the x -coordinates of the points of intersection of

$$y = x(4-x) \quad \text{and} \quad y = x^2(7-x)$$

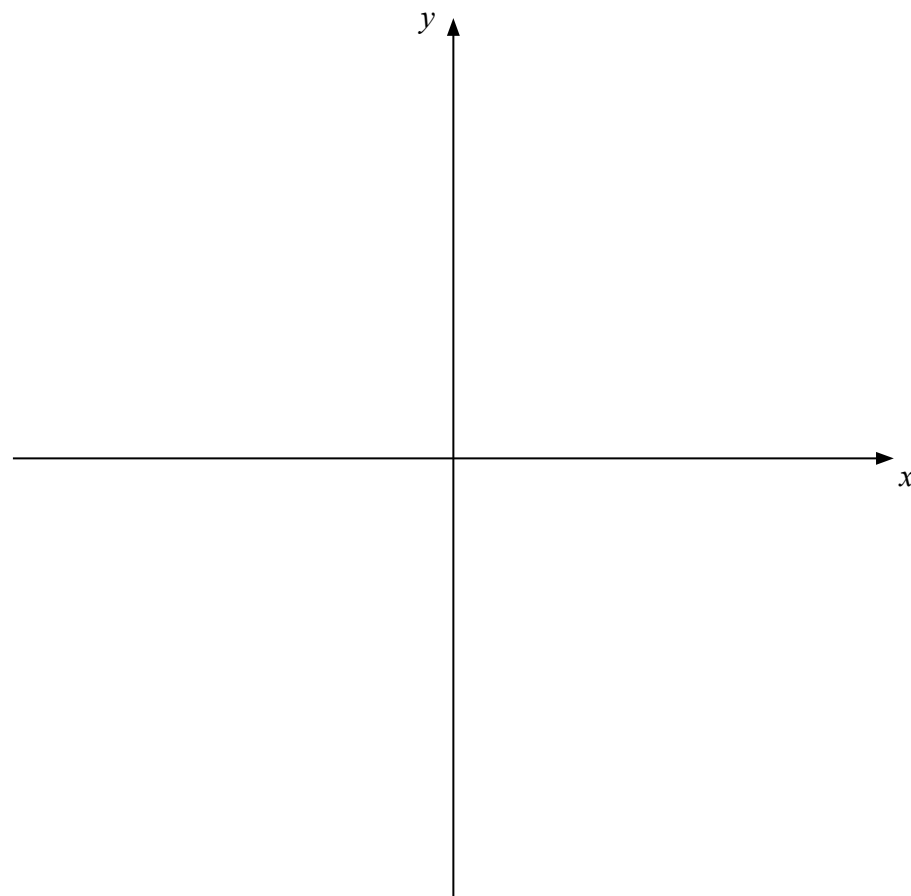
are given by the solutions to the equation $x(x^2 - 8x + 4) = 0$

(3)

The point A lies on both of the curves and the x and y coordinates of A are both positive.

(c) Find the exact coordinates of A , leaving your answer in the form $(p + q\sqrt{3}, r + s\sqrt{3})$, where p, q, r and s are integers.

(7)



11. The curve C has equation $y=f(x)$, $x > 0$, where

$$\frac{dy}{dx} = 3x - \frac{5}{\sqrt{x}} - 2$$

Given that the point $P(4, 5)$ lies on C , find

(a) $f(x)$,

(5)

(b) an equation of the tangent to C at the point P , giving your answer in the form $ax+by+c=0$, where a , b and c are integers.

(4)



